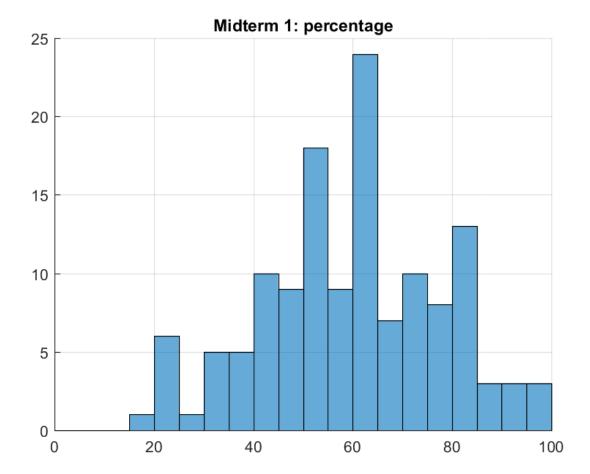
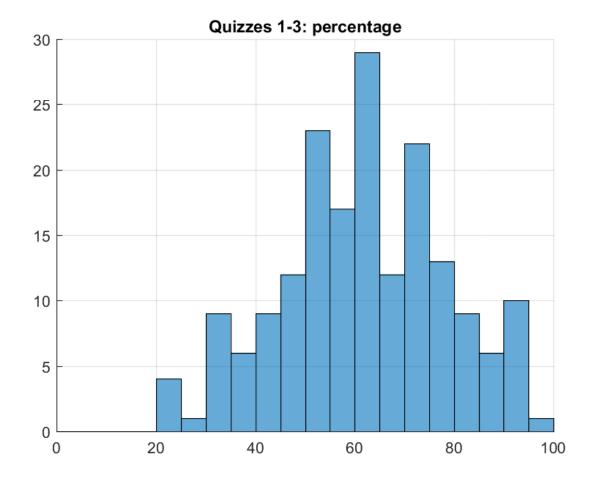
MAT 126.01, Prof. Bishop, Tuesday, Sept. 29, 2020 Discuss Midterm 1 Section 2.2, Volumes by Slicing





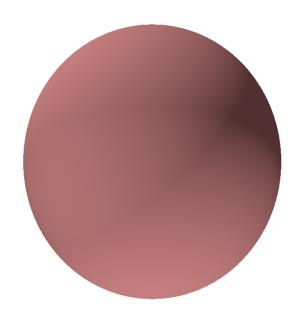
Precalculus volume formulas:

Sphere
$$V = \frac{4}{3}\pi r^3$$

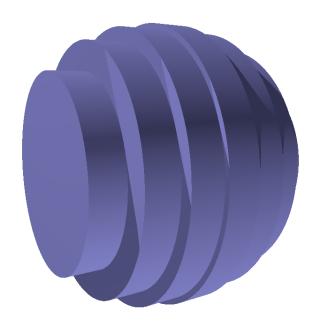
Cone
$$V = \frac{1}{3}\pi r^2 h$$

Pyramid
$$\frac{1}{3}Ah$$

Derive volume of sphere $V = \frac{4}{3}\pi r^3$



Derive volume of sphere $V = \frac{4}{3}\pi r^3$



Derive volume of cone $V = \frac{1}{3}\pi r^2 h$

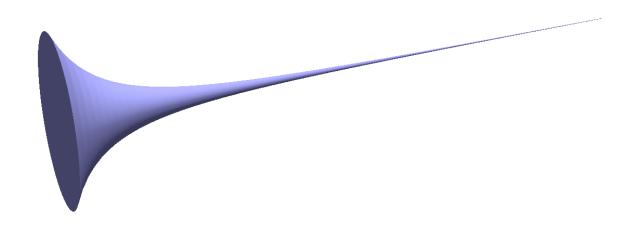
If the graph of $f \ge 0$ on [a, b] is revolved around the x-axis, the volume of the solid obtained is

$$\pi \int_{a}^{b} f(x)^{2} dx.$$

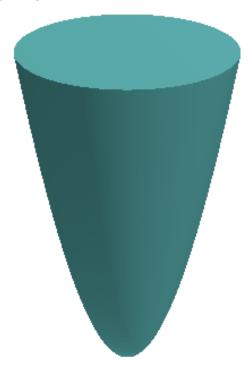
Suppose 1/x on [1,2] is revolved around x-axis. What is the resulting volume?



Suppose 1/x on $[1, \infty)$ is revolved around x-axis. What is the resulting volume?



Suppose x^2 on [0,2] is revolved around y-axis. What is the resulting volume?



Washer method

If $f \ge g \ge 0$ [a, b] and the region

$$\{(x,y): a \le x \le b, g(x) \le y \le f(x)\}$$

is revolved around the x-axis, the volume of the solid obtained is

$$\pi \int_{a}^{b} (f(x)^{2} - g(x)^{2}) dx.$$

Suppose a cylinder of radius 1/2 along the x-axis is removed from a sphere of radius 1 centered at the origin. How much volume remains?

