

Name:

Math 122 (Fall '15)

# Midterm 1

October 1, 2015

1. (15pts)	
2. (15pts)	
3. (15pts)	
4. (15pts)	
5. (20pts)	
6. (20pts)	
Total (100pts)	

1. (15pts) Solve the following equations:

(1)  $5x + 3 = 3x + 5$

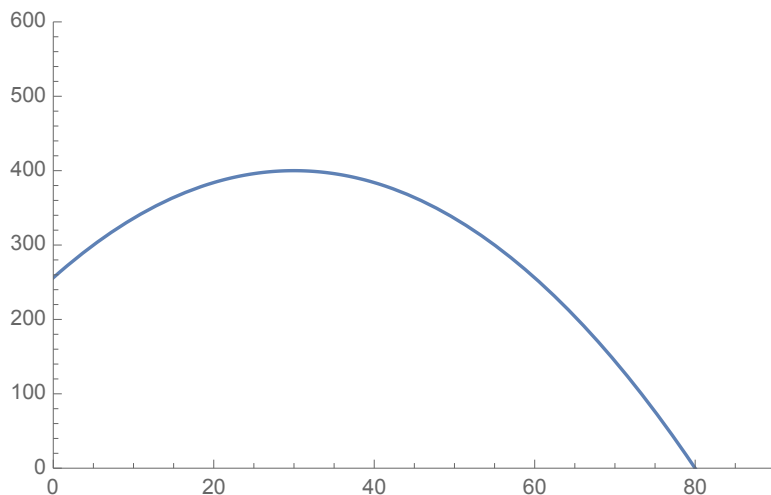
(2)  $x^3 = 4x$

(3)  $\sqrt{x} = 2x^{\frac{1}{3}}$

(4)  $2e^x = 2^x$

(5)  $\ln(x) + \ln(2x) = \ln 3$

**2. (15pts)** The yield,  $Y$ , of an apple orchard (in bushels) as a function of the amount,  $a$ , of fertilizer (in pounds) used on the orchard is shown below.



- (a) Describe the effect of the amount of fertilizer on the yield of the orchard.
  
- (b) What is the vertical intercept? Explain what it means in terms of apples and fertilizer.
  
- (c) What is the horizontal intercept? Explain what it means in terms of apples and fertilizer.
  
- (d) Is the function increasing or decreasing at  $a = 60$ ?
  
- (e) Is the graph concave up or down near  $a = 40$ ?

**3. (15pts)** Assume that \$12,000 are deposited into an account. How long does it take to reach \$20,000 if either

A) the account is paying no interest, but the owner deposits \$1,000 each year.

or

B) the account is paying 8% interest compounded continuously (and no further deposits).

**Note:** *In each of the two cases, write down the function modeling the situation, and solve the corresponding equation.*

4. (15pts) The following table give  $P = f(t)$ , the number of households, in millions, in the US with cable television  $t$  years since 1998

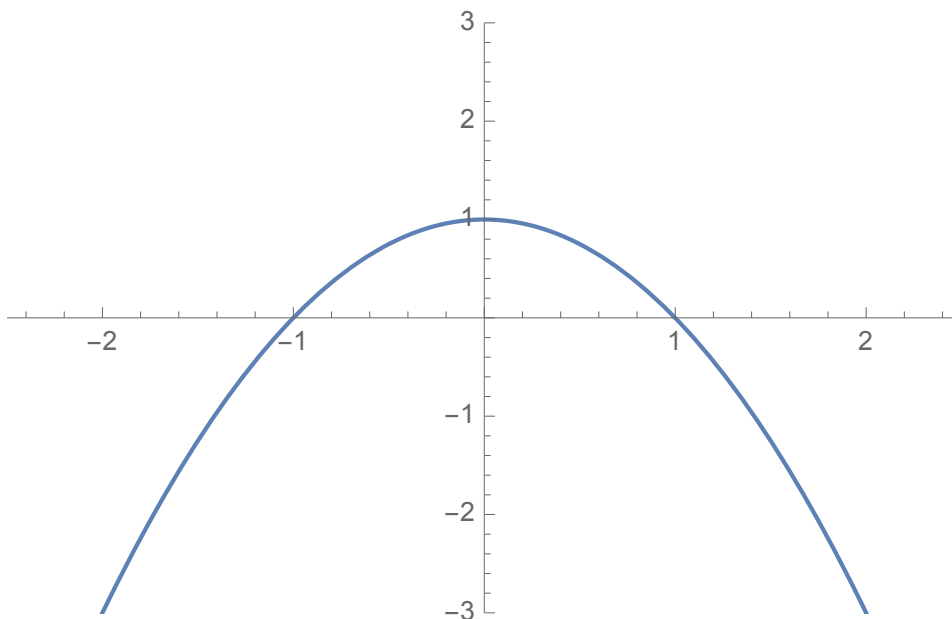
t	0	2	4	6	8	10	12
P	64.65	66.25	66.732	65.727	65.141	64.874	60.958

(i) Does  $f'(6)$  appear to be positive or negative? What does this tell you about the number of households with cable television?

(ii) Estimate  $f'(2)$ . Estimate  $f'(10)$ . Explain what each is telling you, in terms of cable television.

(iii) Is  $f''(4)$  positive or negative? Explain.

5. (20pts) The following is the graph of the first derivative  $f'(x)$ :



- i) Find the intervals on which  $f(x)$  is increasing and those on which  $f(x)$  is decreasing.
  
  
  
  
  
  
  
  
  
  
- ii) Find the intervals on which  $f(x)$  is concave up and those on which  $f(x)$  is concave down.
  
  
  
  
  
  
  
  
  
  
- iii) Assume  $f(0) = 1$ . Which of the following is possible:  $f(1) = 3$  or  $f(1) = 0$ . Explain.

iv) Sketch a graph of  $f''(x)$ .

v) Assume  $f(0) = 1$ . Sketch a graph of  $f(x)$ .

**6. (20pts, 2pts for each question) True/False or Fill-in**

- (1) If  $f(x) = x^2 + 2x + 1$  then  $f(3) = 15$ .
  
- (2) The function  $D = f(r)$  given by  $D = -3r + 10$  is an increasing function of  $r$ .
  
- (3) If the relative rate the change for  $f$  is constant, then  $f$  is \_\_\_\_\_ function.
  
- (4) The average rate of change of a function is the slope of [SELECT ONE]
  - secant between two points on the graph, or
  - tangent at a given point to the graph.
  
- (5) If  $y = f(x)$  then  $\frac{dy}{dx}$  and  $f'(x)$  mean the same thing.
  
- (6) The  $f$  is negative on an interval, then the derivative of  $f$  is decreasing on that interval.
  
- (7) If  $f'' > 0$  on an interval then  $f$  is \_\_\_\_\_ on that interval.
  
- (8) The instantaneous rate of change for  $e^x$  is 1 everywhere.
  
- (9) There is a function with  $f'' = 0$  everywhere.
  
- (10) If your answer to question (9) is YES, give an example. If the answer is NO, explain.